

1. If the sum of a certain number of terms, starting from first, of an A.P 25, 22, 19, ... is 116, find the last term taken in the sum.
2. The sum of first three terms of a G.P is  $\frac{39}{10}$  and their product is 1. Find the first term, the common ratio and the terms of this G.P.
3. If a, b, c are in G.P, prove that  $a^2 + b^2$ ,  $ab + bc$ ,  $b^2 + c^2$  are also in G.P.
4. If  $a^2, b^2, c^2$  are in A.P, then show that  $\frac{1}{b+c}, \frac{1}{c+a}, \frac{1}{a+b}$  are also in A.P.
5. In a sequence the first number is  $\frac{1}{3}$ . The (n+1)th number is nth number divided by one more than the nth number. what is the 50<sup>th</sup> number.
6. Which term of an A.P,  $7 - 4i, 6 - 2i, 5 - 0i, 4 + 2i, \dots$  is (i) purely real (ii) purely imaginary?
7. If m<sup>th</sup> term of an A.P, is  $\frac{1}{n}$  and the nth term is  $\frac{1}{m}$ , show that the sum of first mn terms is  $\frac{1}{2}(mn + 1)$ .
8. Mona buys a car for Rs.22000. She pays Rs.6000 cash and agrees to pay the balance in annual installments of Rs.1000 plus 10% interest on the unpaid amount. Find the total cost of the car.
9. The ratio of the sums of m and n terms of an A.P, is  $m^2 : n^2$ , show that the ratio of mth and nth terms is  $(2m - 1) : (2n - 1)$ .
10. Find four numbers in A.P, whose sum is 10 and the sum of whose squares is 30.
11. Insert 3 arithmetic means between 2 and 10.
12. If a, b, c are in A.P, prove that  $(b + c)^2 - a^2, (c + a)^2 - b^2, (a + b)^2 - c^2$  are also in A.P
13. Insert 4 geometric means between 1 and 243.
14. If the A.M and G.M between two numbers a and b are in the ratio m : n, then prove that the numbers are in the ratio  $m + \sqrt{m^2 - n^2} : m - \sqrt{m^2 - n^2}$ .
15. The sum of three numbers in G.P is 56. If 1, 7, 21 are subtracted from the numbers respectively, the resulting numbers form an A.P. Find the numbers.